

Equations of Lines (slope-intercept form)

slope-intercept form given a situation.

When you have a real world (word problem) that requires you to write an equation in slope intercept form, there are two things that you want to look for:

1. **A Rate.** The rate is your slope in the problem. The following are examples of a rate
 - \$3 per day
 - \$2 an hour
 - 60 mph
 - 2 m/s
 - \$6 a minute
 - 45 words per minute

This number is always related to the x-value.

Per is a key word that is often associated with slope.

2. **A Flat Fee.** A flat fee or starting value is your y-intercept. This value is a constant. It never changes.

Use the chart below to help you organize your information as you analyze each word problem. This will help you to write your equation!

Flat Fee (starting #)	b (y-intercept)	?
Rate	m (slope)	?

Take a look at the examples below to better clarify how this chart can help you!

Example 1

You are visiting Baltimore MD, and a taxi company charges a flat fee of \$3.00 for using the taxi and an additional \$0.75 per mile. Write an equation that you could use to find the cost of a taxi ride in Baltimore, MD. Let x represent the number of miles and y represent the total cost.

- How much would a taxi ride for 8 miles cost?

Flat Fee (starting #)	b (y-intercept)	3
Rate	m (slope)	0.75

$$y = mx + b$$

$$y = .75(x) + 3$$

- The equation could be used to find the cost of a taxi ride in Baltimore, MD is $y = 0.75x + 3$
- To find out the cost for an 8 mile ride, substitute 8 for x.

$$y = \frac{0.75(8) + 3}{6 + 3}$$

\$9

for 8 miles.

$\frac{3}{4} \cdot 8^2$

Example 2

A plumber charges a fee of \$120 to make a house call. He also charges \$10.00 an hour for labor. Write an equation that you could use to find the amount a plumber charges for a house call based on the number of hours of labor. Let x represent the number of hours of labor and y represent the total cost.

- How much would a house call cost that requires 2.5 hours of labor?

Flat Fee (starting #)	b (y-intercept)	120
Rate	m (slope)	10

$$y = mx + b$$

$$y = 10(x) + 120$$

- The equation could be used to find the amount a plumber charges is

$$y = 10x + 120$$

- To find out the cost for the 2.5 hours, substitute 2.5 for x.

$$y = \frac{10(2.5) + 120}{25 + 120}$$

\$145

A plumber would cost \$145 for 2.5 hours.

Your Turn...

- Hannah's electricity company charges her \$0.10 per kWh (kilowatt-hour) of electricity, plus a basic connection charge of \$15.00 each month. Write a linear function that models her monthly electricity bill as a function of electricity usage. Let y represent the cost and x represent the amount of electricity.

- How much would her bill be if she used 500kWh of electricity?

Flat Fee (starting #)	b (y-intercept)	15
Rate	m (slope)	0.10

$$y = mx + b$$

$$y = 0.10(x) + 15$$

- The equation could be used to find the charge on her electric bill is
- To find out the cost for the electricity, substitute 500 for x.

$$y = \frac{0.10(500) + 15}{50 + 15}$$

\$65

A bill would be \$65 for 500kWh.

Homework is continued