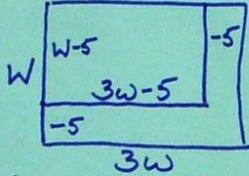


Area Problems; #2

Example:

A rectangle is three times as long as it is wide. If both of the dimensions are decreased by 5m, its area is decreased by 215m^2 . Find its original dimensions.



$$\begin{aligned} \text{Big} - 215 &= \text{Small} \\ W \cdot 3W - 215 &= (3W-5)(W-5) \\ 3W^2 - 215 &= 3W^2 - 15W - 5W + 25 \end{aligned}$$

$$-240 = -20W$$

$$W = 12$$

$$3W = 3 \cdot 12 = 36$$

Problem for practice:

$$12 \times 36\text{m}$$

A rectangle is twice as long as it is wide. If both of the dimensions are decreased by 4m, its area is decreased by 164m^2 . Find its original dimensions.

Write 124 in scientific notation.

This is not a very large number, but it will work nicely for an example. To convert this to scientific notation, I first write "1.24". This is not the same number, but $(1.24)(100) = 124$ is, and $100 = 10^2$. Then, in scientific notation, 124 is written as 1.24×10^2 .

Actually, converting between "regular" notation and scientific notation is even simpler than I just showed, because all you really need to do is

Write in decimal notation

Since the exponent on 10 is "12", I'll need to move the decimal point to the right, 12 places. I'll need to move the decimal point twelve places over. I make little loops when I count off the places.

number, so I'll need to move the exponent on 10 is "12", I'll need to move the decimal point twelve places over. I make little loops

fill in the loops with zeroes:

3,600,000,000,000
1 2 3 4 5 6 7 8 9 10 11 12

In other words, the number

Convert 93,000,000 to

This is a large number, so the "interesting" digit in this number is the leading 9, so that's where I'll start. I'll move the decimal point to the right until I have a decimal point to the right of the 9, so that's where the decimal point will need to move seven places. The answer is 9.3×10^7 .

interesting" digit in this number is the leading 9, so that's where I'll start. I'll move the decimal point to the right until I have a decimal point to the right of the 9, so that's where the decimal point will need to move seven places. The answer is 9.3

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Scientific Notation and Standard Form (Decimal Notation) Practice

Write each number in standard form.

- 1) 4×10^3 4000
- 2) 4.5×10^4 45,000
- 3) 6.5×10^5 650,000
- 4) 6×10^2 760
- 5) 8×10^3 8,000
- 6) 6.32×10^7 63,200,000

Write each number in scientific notation.

- 7) 65,000,000 6.5×10^7
- 8) 98,000,000,000 9.8×10^{10}
- 9) 373,000 3.73×10^5
- 10) 697,000,000,000 6.97×10^{11}
- 11) 54,000,000 5.4×10^7
- 12) 24,340,000 2.434×10^7

Use your calculator to evaluate the following. Write the answer in scientific notation and standard form. Round to three significant digits.

- | | Scientific notation | Standard form |
|-----------|---|-------------------------------|
| 7^{12} | <u>1.38×10^{10}</u> | <u>13,800,000,000</u> |
| 12^{15} | <u>1.54×10^{16}</u> | <u>15,400,000,000,000,000</u> |
| 4^{24} | <u>2.81×10^{14}</u> | <u>281,000,000,000,000</u> |
| 18^9 | <u>1.98×10^{11}</u> | <u>198,000,000,000</u> |